

# D3-brane model building and the supertrace rule

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String Phenomenology

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Work with I. Bena, M. Graña, S. Kuperstein and M. Petrini  
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# Outline

- 1 SUSY gauge theories from D3-branes
- 2 Softly broken  $\mathcal{N} = 1$  theories
- 3 Constraints from supergravity
  - Classical considerations
  - Quantum corrections

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# Motivation

Open string excitations on a stack of  $N$   $D3$ -branes (at a regular point of  $M_{\text{int}}$ ):

$\implies$  Effective field theory of massless modes

- (1/2) of supersymmetry preserved
- gauge group  $U(N)$
- matter content:
  - 4 fermions in the adjoint of  $U(N)$
  - 6 scalars in the adjoint of  $U(N)$

$\implies$   $\mathcal{N} = 4$  super Yang-Mills (SYM)

→ Place  $D3$ -branes at singularities of  $\mathbb{C}^3/\mathbb{Z}_p$

⇒  $U(N) \rightarrow U(pN) \xrightarrow{\text{split}}$  subgroups (quiver diagrams):\*

- SM- or GUT-like gauge groups
- matter fields in bi-fundamental reps.

→ Fluxes on  $M_{\text{int}} \Rightarrow$

- susy-preserving masses
- susy-breaking terms (softly)<sup>†</sup>

Explicit susy-breaking  $\overset{?}{\rightarrow}$  avoid very light susy particles

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\*Douglas, Moore '96

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$$\underline{\mathcal{N} = 4 \text{ SYM: } W = (g/3!) \epsilon_{ijk} \Phi^i \Phi^j \Phi^k}$$

→ Deform it:

- $\mathcal{N} = 4 \longrightarrow \mathcal{N} = 1$  :  $\delta W = (1/2) m_{ij} \Phi^i \Phi^j$
- $\mathcal{N} = 1 \xrightarrow{\text{softly}} \mathcal{N} = 0$  :  $\delta \mathcal{L} = \mathcal{L}_{\text{soft}}(m_{\text{soft}}^2, b_{ij}, \hat{m}_i, \bar{m}, c_{ij}^k, a_{ijk})$

$$\begin{aligned} \mathcal{L}_{\text{susy}} + \mathcal{L}_{\text{soft}} = & -(mm^\dagger)_i^j \phi^i \bar{\phi}_j - \left( \frac{1}{2} m_{ij} \psi^i \psi^j + h.c. \right) \\ & - (m_{\text{soft}}^2)_i^j \phi^i \bar{\phi}_j - \left( \frac{1}{2} b_{ij} \phi^i \phi^j + \hat{m}_i \psi^i \lambda + \frac{1}{2} \bar{m} \lambda \lambda + h.c. \right) \\ & - \left( \frac{1}{2} m_{il} \epsilon^{ljk} \phi^i \bar{\phi}_j \bar{\phi}_k \right. \\ & \left. - \frac{1}{2} c_{ij}^k \phi^i \phi^j \bar{\phi}_k - \frac{1}{6} a_{ijk} \phi^i \phi^j \phi^k + h.c. \right) \end{aligned}$$

→ Good UV behaviour (absence of quadratic divergences)

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→ Good UV behaviour (absence of quadratic divergences)

→ Descends from  $\mathcal{N} = 4$  SYM  $\implies$  memory of  $SU(4)$  R-symmetry

Fermions:

$$M_{IJ}^{\text{ferm}} = \begin{pmatrix} m_{ij} & \hat{m}_i \\ \hat{m}_i^\dagger & \tilde{m} \end{pmatrix} \quad \text{in } \mathbf{10} = \mathbf{6} + \mathbf{3} + \mathbf{1} \quad \text{of } SU(4)_R \supset \underbrace{SU(3)}_{\text{Comp.Str.}} \times U(1)_R$$

→ But  $SU(4) \cong SO(6)/\mathbb{Z}_2 \implies \mathbf{10}$  encoded in  $T_3$  with  $\star T_3 = -iT_3$

$$m_{ij} = \frac{1}{2} T_{i\bar{k}l} \epsilon^{\bar{k}l}{}_j \rightarrow (1,2) \text{ primitive } \quad \mathbf{6}$$

$$\hat{m}_i = -\frac{i}{2} T_{ij\bar{k}} J^j \bar{k} \rightarrow (2,1) \text{ non-prim. } \quad \mathbf{3}$$

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Bosons:

$$(M^2)_{AB}^{\text{bos}} = \left\{ \begin{array}{l} (mm^\dagger + m_{\text{soft}}^2)_{i\bar{j}} \\ \text{Tr}(mm^\dagger + m_{\text{soft}}^2) \\ b_{i\bar{j}} \\ \bar{b}_{i\bar{j}} \end{array} \right\} \quad \text{in } \mathbf{21} = (\mathbf{8} + \mathbf{1})_{+\text{soft}} + \mathbf{6} + \bar{\mathbf{6}}$$

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# Fermion masses and boson trilinear couplings

## IIB sugra background:

$$\rightarrow \text{Metric: } ds_{10}^2 = e^{2\alpha(y)} \underbrace{ds_4^2(x)}_{D3\text{-brane}} + \underbrace{ds_6^2(y)}_{M_{\text{int}}} \leftarrow SO(6)$$

$$\rightarrow 5\text{-form flux: } F_5 = (1 + *_{10}) d\mathcal{C}(y) \wedge \text{vol}_4$$

$$\rightarrow 3\text{-form flux: } G_3 = F_3 - ie^{-\phi} H_3 \quad \longrightarrow \quad T_3 = e^{4\alpha} (*_6 G_3 - iG_3)$$

$$\implies T_3 \text{ position independent!}^*$$

$T_3$  couplings to D-brane **bosons** and **fermions** determine

- **Boson** trilinear couplings<sup>†</sup>:  $T_{ij\bar{k}} = c^k{}_{ij}$  and  $T_{ijk} = a_{ijk}$
- **Fermion** masses<sup>‡</sup>:  $T_{ij\bar{k}} = \delta_{[i}^k \hat{m}_{j]}$  and  $T_{ijk} = \tilde{m} \epsilon_{ijk}$

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# Boson masses

→ Probe D3-brane in equilibrium at  $y^0$  with potential:

$$V = V_0 + 0 + \frac{1}{2}(\partial_{AB}^2 V)(\delta y)^A(\delta y)^B + \dots$$

$$\sim \frac{1}{2}(M^2)_{AB}^{\text{bos}} \phi^A \phi^B$$

with  $V = e^{4\alpha} - \mathcal{C}$

→ Recall:  $M_{\text{bos}}^2 \in \mathbf{20} + \mathbf{1}$

- The  $\mathbf{20}$  is determined by the geometry near the brane, but..
- The trace is fixed by equations of motion\*:  $\text{Tr}(M_{\text{bos}}^2) \propto |T_3|^2$

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# The supertrace rule

Collecting the results:

- $|T_3|^2 = \text{Tr}(mm^\dagger + m_{\text{soft}}^2) = \text{Tr}(M_{\text{bos}}^2)$
- $|T_3|^2 = \text{Tr}(mm^\dagger + 2\hat{m}_i\tilde{m}^i + \tilde{m}^2) = \text{Tr}(M_{\text{ferm}}M_{\text{ferm}}^\dagger)$

$\implies$

$$\text{Tr}[\text{boson masses}^2] = \text{Tr}[\text{fermion masses}^2]$$

$\longrightarrow$  Soft-susy-breaking terms cannot avoid the supertrace rule

## Quantum corrections

- Beta-functions for all couplings of  $\mathcal{L}_{\text{susy}} + \mathcal{L}_{\text{soft}} \longrightarrow \beta_i(\text{susy}; \text{soft})^*$
- In general (arbitrary couplings):  $\beta_i \neq 0$  but..
- For theories on D3-branes (sugra constraints):  $\beta_i = 0$  at 1 and 2 loops  
 (checked also on orbifold singularities ( $\mathbb{C}^3/\mathbb{Z}_2, \mathbb{C}^3/\mathbb{Z}_3$ ))

In particular this means:

$$\implies \text{Tr}(M_{\text{bos}}^2) = \text{Tr}(M_{\text{ferm}}^2) \text{ up to two loops}$$

$\text{Tr}(M_{\text{ferm}}^2)$  does not run (dual to constant  $T_3$ ):

↷ Expect  $\text{Tr}(M_{\text{bos}}^2)$  not to run as well

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# Summary

- D3-branes carry on their world-volume susy gauge theories
- Fluxes induce terms that break susy softly
- Explicitly breaking susy seems to avoid light superpartners
- However, string theory eom require  $\text{Tr}(M_{\text{bos}}^2) = \text{Tr}(M_{\text{ferm}}^2)$
- D3-brane model building problematic for phenomenology

Thank you for your attention!