

Towards global embedding of Fibre inflation

(with the inclusion of higher-derivative α' -corrections)

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June 23, 2016

String Pheno-2016, Ioannina

Work in progress

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Plan

- Some motivations
- Fibre Inflation
- Global embedding: A list of minimal requirements
- Explicit constructions of concrete examples in which Fibre inflation could be realized:
 - Scheme 1: Winding-corrections with F^4 -terms
 - Scheme 2: KK-corrections with F^4 -terms
 - Scheme 3: KK+Winding-corrections with F^4 -terms
- Summary and outlook

Some General Motivations

Some basic requirements for (semi-)realistic model building in string cosmology

- Moduli stabilization and realizing de-Sitter solution
- Embedding inflationary scenarios (solving η -problem) and consistent realization of cosmological observables

Though recent Planck+BICEP2 paper has diluted the original BICEP2 claim on tensor-to-scalar ratio, $r < 0.11$, nevertheless

- Realizing non-trivial r could still be desirable !

Combining cosmo and pheno requirements ! (local/global effects interplay)

- Technical aspects
 - Moduli stabilization and chirality conflict [Blumenhagen, Moster, Plauschinn]
 - Need to sum over all possible instanton contributions, e.g. rigidifying E3-instantons [Bianchi, Collinucci, Martucci] used for realizing dS [Louis, Rummel, Valandro, Westphal]
 - Tadpole/anomaly cancellations, open string moduli, ...
 - Recent updates on warping effects [Martucci], [de Alwis], ...
 - Chiral global embedding on top of moduli stabilization [Cicoli, Krippendorf, Mayrhofer, Quevedo, Valandro],....
- On top of all: Useful control over (un)known α' and g_s corrections ?

Useful control over (un)known α' and g_s corrections ?

- Type IIB Calabi Yau orientifolds: Moduli stabilization better understood
- Symmetries which allow to perform **step-by-step** moduli stabilization
- Helps in creating mass hierarchies, useful e.g. for single field inflation, **analytic computations, or at least numerical control**

In general, K and W can have several corrections induced from various sources,

$$K = K_0 + K_{\alpha'} + K_{g_s} + \dots, \quad W = W_0 + W_{np}^{n=1} + W_{np}^{n=2} + \dots$$

- Effects of string loop-corrections [Berg, Haack, Kors], [Cicoli, Conlon, Quevedo].
- Effects of α' -corrections [Becker, Becker, Haack, Louis], [Grimm, Savelli, Weissenbacher] + [Pedro, Rummel, Westphal], [Ciupke, Louis, Westphal]
- F-theory α'^3 -corrections [Minasian, Pugh, Savelli; see Savelli's talk]

V can also have higher derivatives corrections) [Ciupke, Louis, Westphal; Ciupke's talk]

Apart from conventional need, the new corrections shows the importance of having global constructions. **History:**

- (BBHL) need $\chi(CY) = \int_{CY} c_3(CY)$
- (BHK) need parallel and intersecting stacks of D-branes among $O7$ -planes
- Higher derivative F^4 terms: need $\Pi_i(D_i) = \int_{CY} c_2(CY) \wedge D_i$
- $\chi(CY) \rightarrow \chi(CY) + 2 \int_{CY} D_{O7}^3 = \chi(CY) + 2\chi(D_{O7}) - 2 \int_{CY} c_2(CY) \wedge D_{O7}$:

F-theory α'^3 -corrections.

Useful control over (un)known α' and g_s corrections and the LVS

- The time evolution about the knowledge of these unknown corrections comes out to be quite uncertain. And issue of viability !
- Extensions of "No scale structure" [von Gersdorff, Hebecker], [Berg, Haack, Kors], [Cicoli, Conlon, Quevedo], [Pedro, Rummel, Westphal] !

Consider type IIB superstring theory compactified on an orientifold of a Swiss-Cheese CY with $h_+^{1,1} = 2$, $h_-^{1,1} = 0$ [Balasubramanian+Berglund+Conlon+Quevedo'05].

- Such a CY can be realized as a degree-18 hypersurface inside \mathbb{WCP}^4 [11169] with

- $$\mathcal{V} = \frac{1}{9\sqrt{2}} \left(\tau_b^{3/2} - \tau_s^{3/2} \right) = \gamma_b (T_b + \bar{T}_b)^{3/2} - \gamma_s (T_s + \bar{T}_s)^{3/2}.$$

$$K = -2 \ln(\mathcal{V} + C_{\alpha'}) , \quad W = W_0 + A_s e^{-a_s T_s}$$

- The scalar potential $V = e^K \left(K^{i\bar{j}} (D_i W)(\bar{D}_{\bar{j}} \bar{W}) - 3 |W|^2 \right)$ simplifies into,

$$V(\mathcal{V}, \tau_s) \simeq \frac{2\sqrt{2} a_s^2 A_s^2 \sqrt{\tau_s}}{3\gamma_s \mathcal{V}} e^{-2a_s \tau_s} - \frac{4a_s A_s W_0 \tau_s}{\mathcal{V}^2} e^{-a_s \tau_s} + \frac{3C_{\alpha'} |W_0|^2}{2\mathcal{V}^3}.$$

- LVS minimum: $a_s \tau_s \simeq g_s^{-1}$ and $\mathcal{V} \simeq |W_0| e^{a_s \tau_s}$.

A snapshot of Fiber Inflation [Cicoli+Burgess+Quevedo'08]

The CYs used for this class of models are so-called 'weak' swiss-cheese CYs which have

$$\mathcal{V} = \gamma_b \tau_b \sqrt{\tau_f} - \gamma_s \tau_s^{3/2}; \quad K = -2 \ln(\mathcal{V} + C_{\alpha'}), \quad W = W_0 + A_s e^{-a_s T_s}.$$

The direction in the $(\tau_b - \tau_f)$ -plane orthogonal to the overall volume \mathcal{V} is still flat and is lifted by two-types of string-loop corrections.

- KK-type string-loop corrections: $K_{g_s}^{kk} = g_s \sum_i \frac{C_i^{kk} t_i^\perp}{\mathcal{V}}$
- Winding-type string-loop corrections: $K_{g_s}^w = \sum_i \frac{C_i^w}{\mathcal{V} t_i^\parallel}$

After extended no-scale, the leading order τ_f dependent terms in the scalar potential:

$$V(\tau_f) \simeq \frac{g_s |W_0|^2}{\mathcal{V}^2} \left[\frac{A_1}{\tau_f^2} + \frac{A_2}{\mathcal{V} \sqrt{\tau_f}} + \frac{A_3 \tau_f}{\mathcal{V}^2} \right]$$

Features:

- The inflaton is volume of a $K3$ or \mathbb{T}^4 divisor fibred over a \mathbb{P}^1 base.
- The cosmological parameters $P_s \sim 2.3 \times 10^{-9}$, $n_s \simeq 0.96$ and $N_e \sim 60$ can be successfully realized.
- Moreover, $\epsilon \simeq \frac{3}{2} \eta^2$, $r \sim 6(n_s - 1)^2$, and the best numerical fit can result in r as large as $r \leq 0.007$ (which has improved upto $r \leq 0.01$).

Global embeddings

Global embedding: A list of the minimal requirements



Strategy:

- Searching for some $K3$ -fibred CY threefolds with $h^{1,1} = 3$ and having a shrinkable del-Pezzo divisor (to support LVS).
- Choice of orientifold involutions, tadpole/anomaly cancellations, and fixing a particular Brane-setting.
- Ensuring that the possible brane settings have enough structure (being parallel or intersecting) to generate "appropriate" string-loop corrections.
- Incorporating the effects of recently proposed higher derivative corrections.
- Moduli stabilization and Inflationary dynamics along with the numerics to fit the values without violating the assumptions made.

Searching del-Pezzo divisors: Relevant for LVS

We plan to investigate the CY_3 with $h^{1,1} = 3$ by considering all the 244 polytopes of the [Kreuzer-Skarke list](#) using the recent CY database [\[Altman, Gray, He, Jejjala, Nelson\]](#).

- del-Pezzo surfaces dP_n are realized by [blowing up \$\mathbb{P}^2\$](#) on eight points,

$$dP_n \equiv \begin{array}{ccccc} & & 1 & & \\ & & & & \\ & 0 & & 0 & \\ dP_n \equiv . & 0 & n+1 & 0 & , \quad \forall n \in \{0, 1, \dots, 8\} \\ & 0 & & 0 & \\ & & 1 & & \end{array} \quad \text{[see McAllister's talk]}$$

- A [necessary condition](#) for the divisor D_s to be del-Pezzo is the fact that the only positive triple intersection is the self-intersection, and all the other intersections are either negative or zero. More concretely it is expressed as under,

$$\int_{C=D_i \cap D_s} c_1(D_s) = -D_i D_s^2 > 0 \quad \forall C \neq \emptyset \quad \text{and} \quad i \neq s$$

- For [shrinkability](#), we check if there exist a basis of divisors in which the volume form is (block) diagonal. [Diagonal del-Pezzo and Non-diagonal del-Pezzo](#)
- For $n > 8$, the four-cycles are [rigid but not del Pezzo](#) [\[Cicoli, Kreuzer, Mayrhofer\]](#) and we call them as "[NdP \$_n\$](#) " for notational simplification.

A condition for a $K3$ -fibered CY_3

A theorem in [Oguiso' 92] implies that, if a (numerically effective) divisor D appears linearly in the intersection polynomial, then the CY_3 is a ($K3$ or \mathbb{T}^4) fibration over a \mathbb{P}^1 base.

For D being fibre, out of the possibilities D^3 , $D^2 D_i$ and $DD_i D_j$, the only terms allowed in the intersection polynomial comes out to be $DD_i D_j$, so two possibilities arise,

$$(i). \quad I_3 = \sum_{i \neq f} a_i D_f D_i^2 + \mathcal{P}_1(D_k), \quad \text{where } k \neq f$$

$$(ii). \quad I_3 = \sum_{i \neq j \neq f} a_{ij} D_f D_i D_j + \mathcal{P}_2(D_k) \quad \text{where } k \neq f.$$

$\mathcal{P}_i(D_k)$'s are some cubic polynomials depending on all the divisors but the Fibre D_f .

- "Weak" swiss cheese: Minimal case with $h^{11}(CY) = 3$

$$I_3 = a D_f D_b^2 + b D_s^3 \quad \Longrightarrow \quad \mathcal{V} = \frac{a t_b^2 t_f}{2} + \frac{b t_s^3}{6} = \frac{\tau_b \sqrt{\tau_f}}{\sqrt{2} \sqrt{a}} - \frac{\sqrt{2} \tau_s^{3/2}}{3 \sqrt{b}}$$

- "Weaker" swiss cheese: Minimal case with $h^{11}(CY) = 4$

$$I_3 = a D_f D_x D_y + b D_s^3 \quad \Longrightarrow \quad \mathcal{V} = a t_x t_y t_f + \frac{b t_s^3}{6} = \frac{\sqrt{\tau_x \tau_y \tau_f}}{\sqrt{a}} - \frac{\sqrt{2} \tau_s^{3/2}}{3 \sqrt{b}}$$

This type of volume form has been recently motivated in [Cicoli+Burgess+de Alwis+Quevedo].

Canonical version of the volume form

The intersection polynomial with the divisor basis $\{D_1, D_6, D_7\}$ is:

$$I_3 = 18 D_7^2 D_6 + 81 D_7^3 + 9 D_7^2 D_1 - 3 D_7 D_1^2 + D_1^3$$

which leads to the volume form,

$$\mathcal{V} = \frac{27 t_7^3}{2} + 9 t_7^2 t_6 + \frac{9 t_7^2 t_1}{2} - \frac{3 t_7 t_1^2}{2} + \frac{t_1^3}{6} = \frac{1}{6} \left(\sqrt{\tau_6} (\tau_7 - 2 \tau_6 + 3 \tau_1) - 2 \sqrt{2} \tau_1^{3/2} \right)$$

Switching to the divisor basis $\{D_1, D_6, D_x = D_7 - 2 D_6 + 3 D_1\}$, we have

$$I_3 = D_1^3 + 18 D_6 D_x^2$$

Subsequently, the volume form reduces into the minimal canonical version needed for embedding the Fibre inflation scenario,

$$\mathcal{V} = 9 t_6 t_x^2 + \frac{t_1^3}{6} = \frac{\tau_x \sqrt{\tau_6}}{6} - \frac{\sqrt{2} \tau_1^{3/2}}{3},$$

where

$$t_1 = -\sqrt{2} \sqrt{\tau_1}, \quad t_6 = \frac{\tau_x}{6 \sqrt{\tau_6}}, \quad t_x = \frac{\sqrt{\tau_6}}{3}$$

Higher derivative F^4 -corrections to the scalar potential

Before looking at the relevant Brane-settings satisfying the tadpoles and generating the correct string-loop corrections to the scalar potential, let us fix the higher-order α' correction for this example.

- Knowing the second chern class for this CY to be

$$c_2(CY) = -\frac{14}{3}D_3 D_7 + \frac{2}{3}D_5 D_7 + \frac{8}{3}D_7^2$$

the topological quantities Π_i 's appearing in the higher derivative F-term corrections are given as under [Ciupke, Louis, Westphal],

$$\Pi_i(D_i) = \int_{CY} c_2(CY) \wedge D_i, \quad \text{and} \quad V_{F^4} = \frac{\lambda |W_0|^4 \Pi_i t^i}{\mathcal{V}^4}.$$

- These Π 's have some hierarchy, which is good for inflation [see, Cicoli's talk and Ciupke's talk]

$$\Pi_1 = 10, \quad \Pi_2 = 14, \quad \Pi_3 = 34, \quad \Pi_4 = 24, \quad \Pi_5 = 20, \quad \Pi_6 = 24, \quad \Pi_7 = 126, \quad \Pi_x = 108.$$

- Now considering the relevant one Π_1 , Π_6 and Π_x results in the following scalar potential contribution,

$$V_{F^4} = \frac{\lambda |W_0|^4}{\mathcal{V}^3} \left[\frac{24}{\tau_6} + \frac{8 \sqrt{2} \tau_1^{3/2}}{\tau_6 \mathcal{V}} + \frac{36 \sqrt{\tau_6}}{\mathcal{V}} - \frac{10 \sqrt{2} \sqrt{\tau_1}}{\mathcal{V}} \right]$$

Curves at the intersection of two divisors on the CY hypersurface

	D_1	D_2	D_3	D_4	D_5	D_6	D_7
D_1	---	\mathbb{T}^2	\mathbb{T}^2	\mathcal{C}_2	\emptyset	\emptyset	\mathcal{C}_4
D_2	\mathbb{T}^2	\mathbb{P}^1	\mathbb{T}^2	$2\mathbb{P}^1$	\mathcal{C}_2	\emptyset	\mathcal{C}_4
D_3	\mathbb{T}^2	\mathbb{T}^2	\mathcal{C}_2	\mathbb{P}^1	\mathbb{P}^1	\mathcal{C}_2	\mathcal{C}_{14}
D_4	\mathcal{C}_2	$2\mathbb{P}^1$	\mathbb{P}^1	$6\mathbb{P}^1$	\mathbb{P}^1	\mathcal{C}_2	\mathcal{C}_5
D_5	\emptyset	\mathcal{C}_2	\mathbb{P}^1	\mathbb{P}^1	$4\mathbb{P}^1$	\mathcal{C}_2	\mathcal{C}_5
D_6	\emptyset	\emptyset	\mathcal{C}_2	\mathcal{C}_2	\mathcal{C}_2	\emptyset	\mathcal{C}_{10}
D_7	\mathcal{C}_4	\mathcal{C}_4	\mathcal{C}_{14}	\mathcal{C}_5	\mathcal{C}_5	\mathcal{C}_{10}	\mathcal{C}_{82}



$$t^\cap(D_i \cap D_j) \equiv \int_{CY} J \wedge D_i \wedge D_j =$$

t_1	$-t_1$	$-t_1$	$-2t_1$	0	0	$-3t_1$
$-t_1$	t_1	$6t_x + t_1$	$2(3t_x + t_1)$	$6t_x$	0	$3(6t_x + t_1)$
$-t_1$	$6t_x + t_1$	$4t_x + t_1 + 2t_6$	$2(2t_x + t_1 + t_6)$	$2(t_6 - t_x)$	$6t_x$	$3(6t_x + t_1 + 2t_6)$
$-2t_1$	$2(3t_x + t_1)$	$2(2t_x + t_1 + t_6)$	$2(2t_x + 2t_1 + t_6)$	$2(t_6 - t_x)$	$6t_x$	$6(3t_x + t_1 + t_6)$
0	$6t_x$	$2(t_6 - t_x)$	$2(t_6 - t_x)$	$2(t_6 - 4t_x)$	$6t_x$	$6t_6$
0	0	$6t_x$	$6t_x$	$6t_x$	0	$18t_x$
$-3t_1$	$3(6t_x + t_1)$	$3(6t_x + t_1 + 2t_6)$	$6(3t_x + t_1 + t_6)$	$6t_6$	$18t_x$	$9(8t_x + t_1 + 2t_6)$

Scheme 1: Fibre inflation with winding-type and F^4 -terms

From the curve analysis, we choose the involution $\sigma : x_3 \rightarrow -x_3$.

$$D7 \text{ tadpole : } 8 [O7] \equiv 8 [D_3] = 8 [D_5] + 8 [D_2], \quad \text{D7 not on top of O7}$$

$$\begin{aligned} D3 \text{ tadpole : } N_{D3} + \frac{N_{\text{flux}}}{2} + N_{\text{gauge}} &= \frac{N_{O3}}{4} + \frac{\chi(O7)}{12} + \sum_a \frac{N_a (\chi(D_a) + \chi(D'_a))}{48} \\ &= \frac{5}{4} + \frac{35}{12} + \frac{8(16 + 13)}{48} = 9. \end{aligned}$$

- The relevant intersections to look at are:

$$O7 \cap (D7_a \equiv D_5) = \mathbb{P}^1, \quad O7 \cap (D7_b \equiv D_2) = \mathbb{T}^2, \quad D_a \cap D_b = \mathcal{C}_2.$$

- The scalar potential is

$$V_{g_s}^{(w)} = \sum_i \frac{|W_0|^2 \mathcal{A}_i^w}{\mathcal{V}^3 t_i^\cap} = \frac{|W_0|^2}{\mathcal{V}^3} \left[\frac{\mathcal{A}_1^w}{6 t_x} + \frac{\mathcal{A}_2^w}{(t_1 + 6 t_x)} + \frac{\mathcal{A}_3^w}{2(t_6 - t_x)} \right]$$

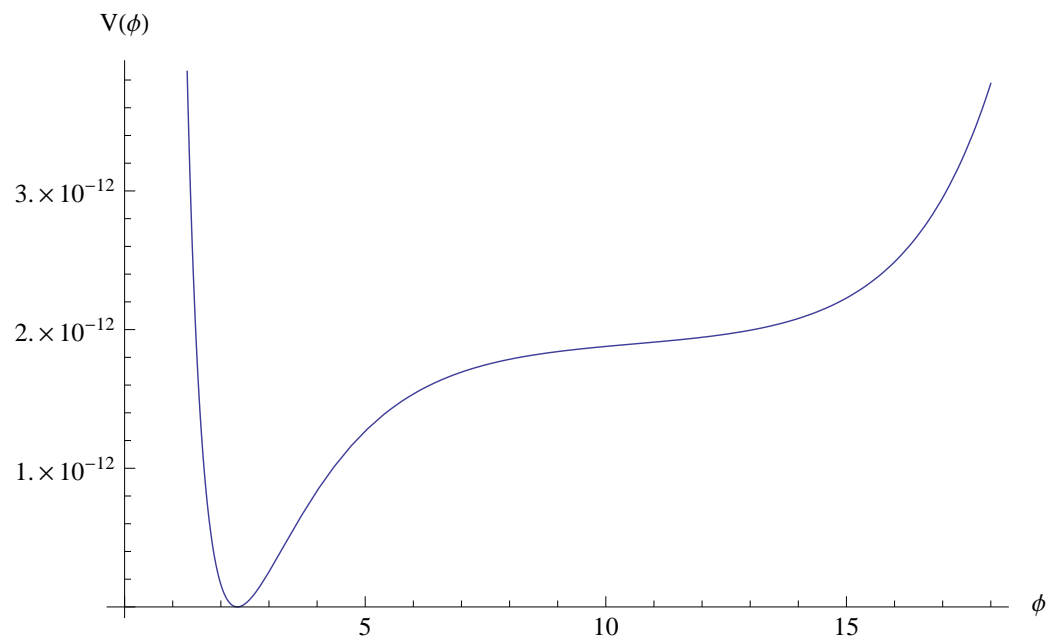
Recalling that $t_6 = \frac{\tau_x}{6\sqrt{\tau_6}}$, $t_1 = -\sqrt{2}\sqrt{\tau_1}$, $t_x = \frac{\sqrt{\tau_6}}{3}$, therefore

$$V_{g_s}^{(w)} = \frac{|W_0|^2}{\mathcal{V}^3} \left[\frac{\mathcal{A}_1^w}{2\sqrt{\tau_6}} + \frac{\mathcal{A}_2^w}{2\sqrt{\tau_6} - \sqrt{2}\sqrt{\tau_1}} \right]$$

Scheme 1: Fibre inflation with winding-type and F^4 -terms

The scalar potential takes the form: $V = V_{up} + V_{LVS} + V_{g_s}^{(w)} + V_{F^4} + \dots$

$$V(\tau_6) \simeq \frac{|W_0|^2}{\mathcal{V}^3} \left[\frac{\mathcal{A}_1^w}{2\sqrt{\tau_6}} + \frac{\mathcal{A}_2^w}{2\sqrt{\tau_6} - \sqrt{2}\sqrt{\tau_1}} \right] + \frac{\lambda |W_0|^4}{\mathcal{V}^3} \left[\frac{24}{\tau_6} + \frac{36\sqrt{\tau_6}}{\mathcal{V}} \right]$$



e.g. $V \simeq V_{up} + \frac{\beta_1}{2\sqrt{\tau_6}} + \frac{\beta_2}{2\sqrt{\tau_6} - \sqrt{2}\sqrt{\tau_1}} + \frac{\beta_3\sqrt{\tau_6}}{\mathcal{V}}; \tau_6 = e^{2\phi/\sqrt{3}},$

Plotted for $\beta_1 = -5, \beta_2 = 2, \beta_3 = 0.001, \tau_1 = 4, \mathcal{V} = 5000$.

For details on Fibre inflation with “Windings + F^4 ”, [see, Cicoli’s talk].

Scheme 2: Fibre inflation with KK-type and F^4 -terms

From the curve analysis, we choose the involution $\sigma : x_6 \rightarrow -x_6$.

$$D7 \text{ tadpole : } 8 [O7] \equiv 8 [D_6] = 8 [D_2] + 8 [D_1], \quad \text{D7 not on top of O7}$$

$$\begin{aligned} D3 \text{ tadpole : } N_{D3} + \frac{N_{\text{flux}}}{2} + N_{\text{gauge}} &= \frac{N_{O3}}{4} + \frac{\chi(O7)}{12} + \sum_a \frac{N_a (\chi(D_a) + \chi(D'_a))}{48} \\ &= \frac{12}{4} + \frac{24}{12} + \frac{8(13 + 11)}{48} = 9. \end{aligned}$$

- The relevant intersections are: $O7 \cap (D7_a \equiv D_2) = \emptyset$, $O7 \cap (D7_b \equiv D_1) = \emptyset$,
 $D_a \cap D_b = \mathbb{T}^2$ but $t^\cap(D_a \cap D_b) = -t_1$ implying no winding-type corrections !
- The string-loop corrections of KK-type are,

$$V_{g_s}^{(kk)} \simeq \frac{|W_0|^2}{\mathcal{V}^2} \left[\frac{g_s^2 \mathcal{B}_6^{kk}}{\tau_6^2} + \frac{g_s^2 \mathcal{B}_x^{kk} \tau_6}{3 \mathcal{V}^2} \right]$$

$$\text{Collecting everything} \implies V = V_{up} + V_{LVS} + V_{g_s}^{(kk)} + V_{F^4} + \dots$$

$$V(\tau_6) = \frac{|W_0|^2}{\mathcal{V}^2} \left[\frac{g_s^2 \mathcal{B}_2^{kk}}{\tau_6^2} + \frac{g_s^2 \mathcal{B}_x^{kk} \tau_6}{3 \mathcal{V}^2} \right] + \frac{\lambda |W_0|^4}{\mathcal{V}^3} \left[\frac{24}{\tau_6} + \frac{36 \sqrt{\tau_6}}{\mathcal{V}} \right]$$

For Fibre inflation with "KK + F^4 " [Broy, Ciupke, Pedro, Westphal], [see also, Ciupke's talk]. We do not find suitable brane settings "just" enough to have standard Fibre inflation (i.e. KK and Winding both).

Scheme 3: Standard Fibre inflation with F^4 -terms

Let us consider the Calabi Yau threefold defined by the following Toric data,

	x_1	x_2	x_3	x_4	x_5	x_6	x_7
6	0	0	1	1	0	3	1
8	0	1	1	1	1	4	0
12	1	0	2	2	1	6	0
	NdP ₁₁	dP_7	SD_2	SD_2	K_3	SD_1	W

$$\text{SR} = \{x_1 x_5, x_2 x_5, x_1 x_3 x_4, x_2 x_6 x_7, x_3 x_4 x_6 x_7\}$$

with Hodge numbers $(h^{2,1}, h^{1,1}) = (111, 3)$ and Euler number $\chi = -216$. This CY corresponds to polytope ID #228 in the database [Altman, Gray, He, Jejjala, Nelson].

The intersection polynomial in the basis of smooth divisors $\{D_2, D_5, D_7\}$, which is subsequently given as under,

$$I_3 = 2D_2^3 + 2D_5 D_7^2 - 8D_7^3 \quad \implies \mathcal{V} = \frac{t_2^3}{3} + t_5 t_7^2 - \frac{4t_7^3}{3} = \frac{1}{6} \left(\sqrt{\tau_5} (3\tau_7 + 4\tau_5) - 2\tau_2^{3/2} \right)$$

For the divisor basis $\{D_2, D_5, D_x = (4D_5 + 3D_7)\}$, the volume simplifies into,

$$\mathcal{V} = 9t_5 t_x^2 + \frac{t_2^3}{3} = \frac{\tau_x \sqrt{\tau_5}}{6} - \frac{\tau_2^{3/2}}{3}, \quad \text{where } t_2 = -\sqrt{\tau_2}, \quad t_5 = \frac{\tau_x}{6\sqrt{\tau_5}}, \quad t_x = \frac{\sqrt{\tau_5}}{3}$$

Scheme 3: Standard Fibre inflation with F^4 -terms

	D_1	D_2	D_3	D_4	D_5	D_6	D_7
D_1	---	\mathbb{T}^2	\mathbb{P}^1	\mathbb{P}^1	\emptyset	\mathcal{C}_4	\mathcal{C}_2
D_2	\mathbb{T}^2	---	\mathbb{T}^2	\mathbb{T}^2	\emptyset	\mathcal{C}_3	\emptyset
D_3	\mathbb{P}^1	\mathbb{T}^2	\mathcal{C}_3	\mathcal{C}_3	\mathcal{C}_2	\mathcal{C}_{19}	$2\mathbb{P}^1$
D_4	\mathbb{P}^1	\mathbb{T}^2	\mathcal{C}_3	\mathcal{C}_3	\mathcal{C}_2	\mathcal{C}_{19}	$2\mathbb{P}^1$
D_5	\emptyset	\emptyset	\mathcal{C}_2	\mathcal{C}_2	\emptyset	\mathcal{C}_{10}	\mathcal{C}_2
D_6	\mathcal{C}_4	\mathcal{C}_3	\mathcal{C}_{19}	\mathcal{C}_{19}	\mathcal{C}_{10}	\mathcal{C}_{93}	$6\mathbb{P}^1$
D_7	\mathcal{C}_2	\emptyset	$2\mathbb{P}^1$	$2\mathbb{P}^1$	\mathcal{C}_2	$6\mathbb{P}^1$	---

$$t^\cap(D_i \cap D_j) \equiv \int_{CY} J \wedge D_i \wedge D_j =$$

$2t_2$	$-2t_2$	$2(t_2 + 3t_x)$	$2(t_2 + 3t_x)$	0	$4t_2 + 18t_x$	$6t_x$
$-2t_2$	$2t_2$	$-2t_2$	$-2t_2$	0	$-4t_2$	0
$2(t_2 + 3t_x)$	$-2t_2$	$2(t_2 + t_5 + 4t_x)$	$2(t_2 + t_5 + 4t_x)$	$6t_x$	$4t_2 + 6(t_5 + 4t_x)$	$2(t_5 - 2t_x)$
$2(t_2 + 3t_x)$	$-2t_2$	$2(t_2 + t_5 + 4t_x)$	$2(t_2 + t_5 + 4t_x)$	$6t_x$	$4t_2 + 6(t_5 + 4t_x)$	$2(t_5 - 2t_x)$
0	0	$6t_x$	$6t_x$	0	$18t_x$	$6t_x$
$4t_2 + 18t_x$	$-4t_2$	$4t_2 + 6(t_5 + 4t_x)$	$4t_2 + 6(t_5 + 4t_x)$	$18t_x$	$8t_2 + 18(t_5 + 4t_x)$	$6(t_5 - 2t_x)$
$6t_x$	0	$2(t_5 - 2t_x)$	$2(t_5 - 2t_x)$	$6t_x$	$6(t_5 - 2t_x)$	$2(t_5 - 8t_x)$

Scheme 3: Standard Fibre inflation with F^4 -terms

From the curve analysis, we choose the involution $\sigma : x_4 \rightarrow -x_4$.

$$D7 \text{ tadpole : } 8 [O7] \equiv 8 [D_4] = 8 [D_5] + 8 [D_1] + 8 [D_7], \quad \text{D7 not on top of O7}$$

$$D3 \text{ tadpole : } N_{D3} + \frac{N_{\text{flux}}}{2} + N_{\text{gauge}} = \frac{N_{O3}}{4} + \frac{\chi(O7)}{12} + \sum_a \frac{N_a (\chi(D_a) + \chi(D'_a))}{48}$$

$$= \frac{2}{4} + \frac{46}{12} + \frac{8(24 + 14 - 4)}{48} = 10.$$

- The string-loop corrections of KK-as well as winding-type are,

$$V_{g_s}^{(kk)} \simeq \frac{|W_0|^2}{\mathcal{V}^2} \left[\frac{g_s^2 \mathcal{B}_5^{kk}}{\tau_5^2} + \frac{g_s^2 \mathcal{B}_x^{kk} \tau_5}{3 \mathcal{V}^2} \right], \quad V_{g_s}^{(w)} = \frac{|W_0|^2}{\mathcal{V}^3} \left[\frac{\mathcal{A}_1^w}{6 t_x} \right] = \frac{|W_0|^2}{\mathcal{V}^3} \left[\frac{\mathcal{A}_1^w}{2\sqrt{\tau_5}} \right]$$

- We have Π_i 's as $\Pi_1 = 140$, $\Pi_2 = 44$, $\Pi_3 = 44$, $\Pi_4 = 8$, $\Pi_5 = 24$, $\Pi_6 = 16$,

$$\Pi_7 = 4, \Pi_x = 108 \text{ which gives } V_{F^4} \simeq \frac{\lambda |W_0|^4}{\mathcal{V}^3} \left[\frac{24}{\tau_5} + \frac{8 \tau_2^{3/2}}{\tau_5 \mathcal{V}} + \frac{36 \sqrt{\tau_5}}{\mathcal{V}} - \frac{8 \sqrt{\tau_2}}{\mathcal{V}} \right]$$

- Collecting things together as: $V = V_{up} + V_{LVS} + V_{g_s}^{(kk)} + V_{g_s}^{(w)} + V_{F^4} + \dots$

$$V(\tau_2) = \frac{|W_0|^2}{\mathcal{V}^2} \left[\frac{g_s^2 \mathcal{B}_5^{kk}}{\tau_5^2} + \frac{\mathcal{A}_1^w}{2 \mathcal{V} \sqrt{\tau_5}} + \frac{g_s^2 \mathcal{B}_x^{kk} \tau_5}{3 \mathcal{V}^2} \right] + \frac{\lambda |W_0|^4}{\mathcal{V}^3} \left[\frac{24}{\tau_5} + \frac{36 \sqrt{\tau_5}}{\mathcal{V}} \right]$$

This is the standard Fibre inflation potential (with F^4 -terms added).

A concrete example of the “weaker” swiss-cheese

Let us consider the following toric data for a Calabi Yau threefold which produces a volume form of kind $\mathcal{V} = \gamma_1 \sqrt{\tau_1 \tau_2 \tau_3} - \gamma_2 \tau_s^{3/2}$,

	x_1	x_2	x_3	x_4	x_5	x_6	x_7	x_8
4	0	0	0	1	1	0	0	2
4	0	0	1	0	0	1	0	2
4	0	1	0	0	0	0	1	2
8	1	0	0	1	0	1	1	4
	dP_7	NdP_{11}	NdP_{11}	$K3$	NdP_{11}	$K3$	$K3$	

$$\text{SR} = \{x_1 x_4, x_1 x_6, x_1 x_7, x_2 x_7, x_3 x_6, x_4 x_5 x_8, x_2 x_3 x_5 x_8\}$$

with $(h^{2,1}, h^{1,1}) = (98, 4)$ and Euler number $\chi = -188$. This corresponds to polytope ID #1206 in the database of [Altman, Gray, He, Jejjala, Nelson].

- The Intersection Polynomial:

$$I_3 = 2 D_1^3 + 2 D_4 D_6 D_7 \implies \mathcal{V} = \frac{t_1^3}{3} + 2 t_4 t_6 t_7.$$

- Subsequently, the overall volume of the CY:

$$\mathcal{V} = \frac{\sqrt{\tau_4 \tau_6 \tau_7}}{\sqrt{2}} - \frac{1}{3} \tau_1^{3/2}.$$

This form can be useful for chiral global embedding of Fibre inflation, work in progress.

Summary and outlook

- Some explicit CY orientifold constructions for (possibly) realizing the standard as well as the modified versions of the Fibre inflation potentials have been presented.
- The recently proposed higher derivative corrections have been investigated for specific models, especially the values of parameters Π) i,s .
- We presented 3 schemes with Brane-settings satisfying the tadpole cancellations
 - Scheme 1: Winding-corrections with F^4 -terms
 - Scheme 2: KK-corrections with F^4 -terms
 - Scheme 3: KK+Winding-corrections with F^4 -terms
- On the lines of recent interest proposed in [Cicoli, Burgess, de Alwis, Quevedo], an explicit CY example having the volume form to be of a 'weaker' swiss-type (which is analogous to the blow-up added version of the toroidal case, e.g. $\mathbb{T}^6/(\mathbb{Z}_2 \times \mathbb{Z}_2)$) has been presented.
- Our aim is to scan the full Calabi Yau database with $h^{1,1} = 3$ and $h^{2,1} = 4$ to look for K3-fibrations with a 'shrinkable' del-Pezzo divisor to list **all** the such weak/weaker swiss-cheese volume forms.
- To understand the KK string-loop corrections better?? and to look for chiral global embedding.