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Non-perturbative *SUSY* and \mathcal{R} -symmetry breaking ;
Inflationary behavior of the no-scale effective *SUGRAS*

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Work to appear (with D. Lüst) . See also

C. Kounnas, D. Lüst and N. Toumbas, Fortsch.Phys. 63 (2015) 12 ; arXiv:1409.7076

1. Introduction

This work is motivated by the observation that many of the superstring theories with **spontaneously broken susy** define at low energies effective theories in a flat Minkowski space-time similar to the **no-scale supergravity models** characterized by :

$$V \geq 0 \quad \text{with} \quad \text{classically untetermined} \quad m_{3/2}(T, U, S, \dots \text{moduli})$$

Cremmer, Ferrara, Kounnas, Nanopoulos⁸², Ellis, Kounnas, Nanopoulos^{83,84},
Ellis, Lahanas, Nanopoulos, Tamvakis⁸⁴...

The minimal $\mathcal{M}_n = SU(1, 1 + n)/U(1) \times SU(1 + n)$ no-scale model is extended by **other moduli fields of the string theory** like:

The dilaton field S , the complex structure fields U_I, \dots :

Witten⁸⁵, Ferrara, Kounnas, Porrati⁸⁶, Ferrara, Kounnas, Zwirner⁹⁴, ...

$$K = -3 \log Y(\psi^I) - \log(S + \bar{S}) - \log(U_1 + \bar{U}_1) - \log(U_2 + \bar{U}_2) - \log(U_3 + \bar{U}_3) + \dots$$

$\psi^I \equiv \{T, \Phi^i\}$ denote the fields of the \mathcal{M}_n manifold

$$Y(\psi^I) = T + \bar{T} - |\Phi^i|^2$$

When the superpotential is independent of T the F -part of the potential is positive semi-definite $V_F \geq 0$ thanks to the no-scale structure of the \mathcal{M}_n sub-manifold.

Ellis, Kounnas, Nanopoulos⁸⁴, Ferrara Kounnas Zwirner⁹⁴...

$$V_F = \frac{3Y \sum_i |W_{\Phi^i}|^2 + |W - (S + \bar{S})W_S|^2 + \sum_I |W - (U_I + \bar{U}_I)W_{U_I}|^2}{Y^3 (S + \bar{S})(U_1 + \bar{U}_1)(U_2 + \bar{U}_2)(U_3 + \bar{U}_3)} \geq 0$$

The positive semi-definite structure of V_F follows from the properties of the $SU(1, n)$ Kähler manifold and the particular $SU(1, 1)_{S, U_I}/U(1)$ manifolds of the (S, U_I) -moduli.

The negative contribution, $-3e^K |W|^2$, of the $N = 1$ sugra potential is cancelled by the contribution of $\psi \equiv \{T, z^i\}$ fields in V_F provided W is T independent.

$$G = K + \log |W|^2, \quad W_T = 0$$

$$e^K \left(G_\psi K^{\psi\bar{\psi}} G_{\bar{\psi}} - 3 \right) |W|^2 = \sum_i \left(\frac{3|W_{\Phi^i}|^2}{Y^2} \right) \frac{1}{(S + \bar{S})(U_1 + \bar{U}_1)(U_2 + \bar{U}_2)(U_3 + \bar{U}_3)}$$

The D -part of the potential is always positive semi-definite $V_D \geq 0$

$$V_D = \sum_\alpha g_\alpha^2 \left[G_A (T^\alpha)_B^A z^B \right]^2 \geq 0, \quad z^B = \{T, \Phi^i, S, U^I, \dots\}.$$

The only way to obtain non-trivial susy-breaking contributions from the D -terms is when they are associated to the gauging of $U(1)_R$ symmetries under which the superpotential W transforms non-trivially under $U(1)_R$:

$$U(1)_R : \quad W \longrightarrow e^{i\xi_W \theta_R} W, \quad \Phi \longrightarrow e^{i\xi_\Phi \theta_R} \Phi$$

In these specific cases a Fayet-Iliopoulos term is generated giving rise to a non trivial (metastable) de Sitter vacua Kounnas, Lüst, Toumbas¹⁴, Ferrara, Kehagias, Porrati¹⁴ ...

$$V_D = \frac{1}{2} g_R^2 \left(\xi_W + 3\xi_\Phi \frac{|\Phi|^2}{Y} + \dots \right)^2$$

The “... ” stand for the contribution of the other fields T, S, U_I, \dots

2 . D -breaking: The emergence of the $\mathcal{R}^2 + \tilde{\xi}\mathcal{R}$ gravity

Dictated by string theory a common form of the superpotential for large T

$$W = A_{ijk} \Phi^i \Phi^j \Phi^k + w(S, U_I) \equiv [\Phi^3] + w .$$

it contains two typical terms:

i) the R -symmetric susy terms $[\Phi^3]$

ii) the w -terms which can be generated by fluxes and/or non-perturbative terms:

$$w = \hat{w} e^{-\beta S}$$

The initial $U(1)_R$ symmetry is generically broken by the w -terms.
 It can be restored if $U(1)_R$ acts nontrivially on w or when w is trivial.

$$U(1)_R : \quad \Phi \longrightarrow e^{i\xi_\Phi \theta_R} \Phi \quad w \longrightarrow e^{i\xi_W \theta_R} w ; \quad \xi_W = 3\xi_\Phi , \quad \text{OR} \quad w \equiv 0.$$

Although the classical $U(1)_R$ is restored in both cases, at the quantum level $U(1)_R$ is anomalous due to its action on the chiral fermions (the susy partners of Φ_i).

It is therefore necessary for the anomaly cancellation to extend the action of $U(1)_R$ to T field as axion translation : Kounnas, Lüst, Toumbas¹⁴

$$U(1)_R : \quad T \longrightarrow T + i\xi_T \theta_R \quad \text{with} \quad \xi_T = \text{Tr } Q$$

For $w \equiv 0$, V_D becomes the only relevant part and has the well known form of the Starobinsky inflationary potential for $W_{\Phi^i} = 0$ (and $W = 0$ since $\xi_\Phi \Phi^i W_{\Phi^i} = 3W$)

$$V = (V_F + V_D) |_{W_{\Phi^i}=0} = \mu^2 \left(1 - \tilde{\xi} e^{-\alpha\phi} + \hat{\Phi}_i^2 \right)^2 ; \quad \tilde{\xi} = \begin{pmatrix} \xi_T \\ \xi_\Phi \end{pmatrix}, \quad \mu^2 = \frac{1}{2} g^2 (3\xi_\Phi)^2$$

In terms of canonically normalized fields,

$$\hat{\Phi}_i = \Phi_i e^{-\frac{\alpha}{2}\phi}, \quad \alpha\phi = \log Y, \quad Y = (T + \bar{T} - |\Phi|)^2 ; \quad \alpha = \sqrt{\frac{2}{3}},$$

the action in the Einstein frame in terms of the no-scale modulus ϕ and Φ_i or $\hat{\Phi}_i$:

$$S_E = \int d^4x \sqrt{|g|} \times$$

$$\frac{1}{2} \left[\mathcal{R} - \partial_\mu \phi \partial^\mu \phi - e^{-\alpha\phi} \partial_\mu \Phi_i \partial^\mu \Phi_i - 2\mu^2 \left(1 - \tilde{\xi} e^{-\alpha\phi} + \hat{\Phi}_i^2 \right)^2 - 2V_F(\hat{\Phi}_i; S, U_I, \dots) + \dots \right]$$

- When $\tilde{\xi} = 0$ the full classical action is invariant under a scale symmetry:

$$\alpha\phi \rightarrow \alpha\phi + 2\sigma, \quad \Phi_i \rightarrow e^\sigma \Phi_i, \quad g_{\mu\nu} \rightarrow g_{\mu\nu},$$

(V_F is function of $\hat{\Phi}_i$; there is no dependence on ϕ in the classical action !)

- When $\tilde{\xi} \neq 0$ The vacuum structure changes drastically. The scale violating term $\{-\tilde{\xi}e^{-\alpha\phi}\}$ induces a slow inflationary transition

de Sitter phase $\langle \mathcal{R} \rangle = 4\mu^2 \longrightarrow$ flat susy phase $\langle \mathcal{R} \rangle = 0$.

The off-shell potential has three characteristic phases: Kounnas, Lüst, Toumbas¹⁴

- (i) Approximate de Sitter phase with negligible scale breaking term $\tilde{\xi}e^{-\alpha\phi} \ll 1$.
In this phase $\hat{\Phi}_i = 0$ thanks to the induced de Sitter mass $m_i^2 = \frac{2}{3}\mu^2$.
The supersymmetry is broken by the $U(1)_R$ Fayet-Iliopoulos D -term; ($V_F = 0$).
- (ii) Flat-Minkowski supersymmetric vacuum with $W_{\Phi^i} = 0$, $3W = \xi_{\Phi} \Phi^i W_{\Phi^i} = 0$
which are satisfied with $\hat{\Phi}_i = 0 \longrightarrow SU(n)$ -symmetric vacuum with $\tilde{\xi}e^{-\alpha\phi} \sim 1$.
- (iii) Scale-breaking dominant phase with $\xi e^{-\alpha\phi} \gg 1$; $|\hat{\Phi}_i|^2 \neq 0$, with broken $SU(n)$
Here also the vacuum is supersymmetric since $W_{\Phi^i} = 0$, $3W = \xi_{\Phi} \Phi^i W_{\Phi^i} = 0$.

Therefore the $w = 0$ case provides an interesting slow inflationary transition very similar to the $SU(1, n)$ -supersymmetric extension of the minimal Starobinsky model:

$$\tilde{\xi}\mathcal{R} + \mathcal{R}^2 + (\Phi\text{-matter}) + (S, U_I + \dots)\text{-moduli terms.}$$

Utilizing the equations of motion for Φ^i, S, U_I

$$\longrightarrow W_{\Phi^i} = 0, \quad 3W = \xi_{\Phi} \Phi^i W_{\Phi^i} = 0 \quad \text{and} \quad T - \bar{T}, S, U_I = \text{const.}$$

we obtain in the Jordan frame the conformally equivalent action setting:

$$g_{\mu\nu} \rightarrow g_{\mu\nu} e^{\log(2t + \tilde{\xi} - |\Phi^i|^2)}, \quad 2t \equiv T + \bar{T} - \tilde{\xi} :$$

$$S_J = \int d^4x \sqrt{|g|} \left\{ \frac{1}{2} \left(2t + \tilde{\xi} - |\Phi^i|^2 \right) \mathcal{R} - 4\mu^2 t^2 - 3 g^{\mu\nu} \partial_{\mu} \Phi^i \partial_{\nu} \bar{\Phi}_i \right\}$$

In this frame the t field appears as a Lagrange multiplier and so,

t can be eliminated by its algebraic equation of motion to obtain:

$$S_J = \int d^4x \sqrt{|g|} \left\{ \frac{1}{2} \left(\frac{\mathcal{R}^2}{8\mu^2} + (\tilde{\xi} - |\Phi^i|^2)\mathcal{R} \right) - 3 g^{\mu\nu} \partial_\mu \Phi^i \partial_\nu \bar{\Phi}_i \right\}$$

Notice that the $\tilde{\xi}$ -term originated by the gauging of the T -translation, and which is necessary for the $U(1)_R$ anomaly cancelation, violates the scale invariance.

- Although the $w = 0$ it gives interesting slow inflationary transition, the over all output it is not satisfactory !
- In the final Flat-Minkowski vacuum the susy turns out to be unbroken !!!
- Many experts in our field think that this is a general statement !
- The main obstruction however comes from the property that if in the final Flat-Minkowski vacuum $W_{\Phi^i} = 0$ implies that $3W = \xi_{\Phi} \Phi^i W_{\Phi^i} = 0$ as well !

This imposes that $m_{3/2} = 0$; susy is always unbroken in the final Flat-Minkowski vacuum.

Can we bypass this obstruction in the cases where $w \neq 0$? (see later)

3. F -susy breaking via fluxes: Absence of R -symmetry Flat no-scale realization

When $w \neq 0$ the $W_{\Phi^i=0}$ minimization does not implies $W = 0$.

Only the susy part $[\Phi^3] = 0 \longrightarrow \langle W = 0 + w \rangle$,

thanks again to the “magic” properties of the $\mathcal{M}_n \psi$ sub-manifold.

Assuming non-trivial fluxes, (similar to those appearing in type IIB), a non-trivial w can be generated, (like for instance)

Derendinger, Kounnas, Zwirner⁰⁴, Derendinger, Kounnas, Petropoulos, Zwirner⁰⁴

$$w = A(S + \epsilon U_1)(U_2 + \epsilon U_3), \quad \epsilon = \pm 1.$$

The F -part of the potential is always positive semi-definite $V_F \geq 0$.

For $\epsilon = -1$, the susy is unbroken with $V_F = 0$,

$$\epsilon = -1 : \quad S = U_1, \quad U_2 = U_3, \quad \text{with} \quad m_{3/2}^2 = 0.$$

For $\epsilon = 1$ the susy is broken with $V_F = 0$,

$$\epsilon = 1 : \quad S = \bar{U}_1, \quad U_2 = \bar{U}_3, \quad \text{with} \quad m_{3/2}^2 = \frac{|\hat{A}|^2}{Y^3}$$

Here we recover the structure of the no-scale models where the susy breaking scale depends on the moduli T which is undetermined at the classical level.

The classical degeneracy of the vacuum is fixed at the quantum level.

Ellis, Kounnas, Nanopoulos^{83,84}, Ellis, Lahanas, Nanopoulos, Tamvakis⁸⁴...

The above example is generic in superstrings when fluxes and (non-) perturbative effects are included. However, when $w \neq 0$ R -symmetry is generically broken.

This implies the absence of D -breaking via Fayet-Iliopoulos term which can induce a (metastable) de Sitter phase and slow inflationary transition of Starobinsky type.

3. D -and F -breaking: Non-perturbative R -symmetry

Including the typical non-perturbative term

$$w = \hat{w} e^{-\beta S}$$

the R -symmetry is restored provided that under $U(1)_R$ S is transforming non-trivially while \hat{w} is neutral.

$$U(1)_R : \quad S \longrightarrow S + i\xi_S \theta, \quad \hat{w} \longrightarrow \hat{w}; \quad \xi_S = -\frac{\xi_W}{\beta} = -3\frac{\xi_\Phi}{\beta}$$

The non-perturbative effects originating from gaugino condensation are of the form

$$w = \mu^3 \exp\left(-\frac{24\pi^2 S}{|b_0|}\right), \quad \Re S = g^{-2}(\mu); \quad \beta = \frac{24\pi^2}{|b_0|}$$

where b_0 is a one-loop beta-function coefficient.

Dine, Rohm, Seiberg, Witten⁸⁵, Derendinger, Ibanez, Nilles^{85,86}, Derendinger, Kounnas, Petropoulos⁰⁶, ...

The expectation value of w defines the renormalization-group-invariant scale Λ of the confining gauge group in which gauginos condense, $\langle w \rangle = \Lambda^3$.

The renormalization scale μ is in general a modulus-dependent quantity.

Derendinger, Kounnas, Petropoulos^{83,84}, ...

At the one-loop level (or in $N = 2$ theories to all orders) μ is independent of S .

At higher orders a non-trivial S -dependence appear.

In the case of a spectator gauge group like the E'_8 in the heterotic
 (only vector multiples in the E'_8 gauge sector)
 all the perturbative corrections can be included, since the exact β -function is known.

$$-\frac{\beta(g)}{g} = \frac{b_0 \left(\frac{g^2}{16\pi^2} \right)}{1 - \frac{b_0}{3} \left(\frac{g^2}{16\pi^2} \right)} \longrightarrow \Lambda^3 = \hat{\mu}^3 (S + \delta) e^{-\beta S}$$

If in the gauge sector there is an extra charged matter then (up to two loop-level)

$$\Lambda^3 = \hat{\mu}^3 (S + \delta)^{1 + \frac{\gamma_m}{b_0}} e^{-\beta S}$$

The explicit appearance of S is in general an obstruction to the R -symmetry
 except iff the δ -term is linear in some of the U_I .

Restricting to the case of $\gamma_m = 0$ and choosing the simplest example of w :

$$w = A (U_2 + U_3) (S + U_1 - 2\beta\gamma) e^{-\beta S} = \hat{w} e^{-\beta S}, \quad \hat{w} = A (U_2 + U_3) (S + U_1 - 2\beta\gamma).$$

The requirements concerning the R -symmetry are satisfied provided that
 U_1 transforms non trivially under $U(1)_R$

$U(1)_R : U_1 \longrightarrow U_1 + i\xi_1 \theta$ with $\xi_1 = -\xi_S$ so that $\hat{w} \longrightarrow \hat{w}$
and also,

$$U(1)_R : \Phi^i \longrightarrow \Phi^i e^{i\xi_\phi \theta}, \quad T \longrightarrow T + i\xi_T \theta, \quad U_{2,3} \longrightarrow U_{2,3} + i\xi_{2,3} \theta$$

$$\text{with : } \quad \xi_W = 3\xi_\Phi = -\beta\xi_S, \quad \xi_1 = -\xi_S, \quad \xi_2 = -\xi_3$$

The total potential is a sum of positive semi-definite terms.

The minimization conditions with $V = 0$ simplifies enormously:

$$i) \quad V_{\Phi^i} = 0 \quad \rightarrow \quad W_\Phi = [\Phi]_{\Phi^i}^3 = 0 \quad \longrightarrow \quad W = \hat{w} e^{-\beta S}$$

$$ii) \quad V_{U_2} = 0 \quad \rightarrow \quad W - (U_2 + \bar{U}_2)W_{U_2} = (-\bar{U}_2 + U_3)\hat{w}e^{-\beta S} = 0 \quad \longrightarrow \quad \bar{U}_2 = U_3$$

$$iii) \quad V_{U_3} = 0 \quad \rightarrow \quad W - (U_3 + \bar{U}_3)W_{U_2} = (-\bar{U}_3 + U_2)\hat{w}e^{-\beta S} = 0 \quad \longrightarrow \quad U_2 = \bar{U}_3$$

$$iv) V_{U_1} = 0 \rightarrow W - (U_1 + \bar{U}_1)W_{U_1} = 0 \quad \longrightarrow \quad (S + U_1 - 2\beta\gamma) = (U_1 + \bar{U}_1)$$

$$v) V_S = 0 \rightarrow W - (S + \bar{S})W_S = 0 \quad \longrightarrow \\ (\bar{S} + U_1 - 2\beta\gamma) = (S + \bar{S}) - \beta(S + \bar{S})(S + U_1 - 2\beta\gamma)$$

The above equations have to be taken together with the constrain $V_D = 0$ which can be seen as $V_{z^I} = 0$ condition for all fields $z^I = (T, \Phi, U_I, S)$,

$$vi) V_D = 0 \rightarrow \frac{1}{2}g_R^2 \left(\frac{3\xi_\Phi |\Phi^i|^2}{Y} - \frac{3\xi_T}{Y} - \frac{\xi_S}{(S + \bar{S})} - \sum_I \frac{\xi_I}{(U_I + \bar{U}_I)} - \beta\xi_S \right)^2 = 0.$$

Combining *iv* with *v*

$$(S + \bar{S}) - (U_1 + \bar{U}_1) - \beta(S + \bar{S})(U_1 + \bar{U}_1) = 0 \quad \longrightarrow \quad \left(\frac{-\xi_S}{(S + \bar{S})} + \frac{\xi_S}{(U_1 + \bar{U}_1)} - \beta\xi_S \right) = 0$$

Combining ii with iii

$$(U_2 + \bar{U}_2) - (U_3 + \bar{U}_3) = 0 \quad \rightarrow \quad \left(\frac{-\xi_2}{(U_2 + \bar{U}_2)} + \frac{\xi_2}{(U_3 + \bar{U}_3)} \right) = 0$$

Inserting to vi we observe that $V_D = 0$ implies that in the global vacuum $|\Phi^i|^2$ is fixed while T remains flat direction.

$$|\Phi^i|^2 = \tilde{\xi}; \quad \tilde{\xi} = \xi_T / \xi_\Phi \quad \text{and} \quad T \text{ arbitrary.}$$

- It is important to stress here that this property, although derived in a particular example, turns out to be generic for all models with R -symmetric w of the type $w = \hat{w} e^{-\beta S}$!

In the example under consideration

(setting $S = s + ia$, $U_1 = u + ib$ and $2\beta\gamma$ real) :

$$u = s - 2\beta\gamma, \quad a = -b \quad \text{and} \quad (s - u) = 2\beta su, \quad \rightarrow \quad su = \gamma$$

$$s = \sqrt{(\beta^2\gamma^2 + \gamma)} + \beta\gamma, \quad u = \sqrt{(\beta^2\gamma^2 + \gamma)} - \beta\gamma.$$

,
 Both the real parts of S and U_1 are fixed while
 their imaginary values are restricted so that $a + b = 0$.

The gravitino mass at the minimum $V = 0$ reads :

$$m_{3/2}^2 = \frac{|\hat{w}|^2 e^{-2\beta s}}{4\gamma Y^3} \neq 0, \quad Y = (T + \bar{T} - |\Phi^i|^2) = 2t - \tilde{\xi}$$

with

$$\hat{w} = 2A(s - 2\beta\gamma) = 2Au$$

There is no-dependence on U_2, U_3 . The effective theory is just the $SU(1, 1 + n)$
 no scale model with a constant term in W proportional to Λ^3 giving rise to
 naturally small susy breaking scale:

$$m_{3/2}^2 = \frac{|\Lambda|^6}{(T' + \bar{T}')^3}, \quad T' + \bar{T}' = T + \bar{T} - \tilde{\xi}.$$

4. Inflationary transitions

The off-shell inflationary properties of the potential $V = V_F + V_D$ depends crucially on the initial values of the fields T, Φ^I, S and U_I .

Assuming $1/g_R^2 = S + \bar{S}$, V_F and V_D scale like:

$$V_F \sim \frac{[\Phi_i^4]}{Y^2 s u u_2 u_3} + \frac{e^{-2\beta s}}{Y^3 s u}, \quad V_D \sim \frac{1}{s}$$

- For large $Y = e^{\alpha\phi}$ the potential is exponentially dominated by V_D .
- The V_D dominance is even more efficient in the large S -limit.

It follows that depending on the initial off-shell values of T, Φ^I, S and U_I the inflationary transitions can be either:

- Fast transition giving rise to “multi component chaotic inflationary models”

OR

- Exponentially slow transition giving rise to slow-roll inflation from
de Sitter \longrightarrow flat space.

Setting for instance S and $U_{2,3}$ and to their minima with $s = g_R^{-2}$ and $U_2 = \bar{U}_3$:

$$V \sim \frac{1}{2} g_R^2 (3\xi_\Phi)^2 \left(|\hat{\Phi}^i|^2 - \tilde{\xi} e^{-\alpha\phi} - \frac{1}{\beta} e^{-\sqrt{2}\phi_u} + \hat{\xi} \right)^2 \longrightarrow \mu^2 = \frac{1}{2} g_R^2 (3\xi_\Phi)^2 (\hat{\xi})^2$$

$$\hat{\xi} \equiv \left(1 + \frac{1}{2\beta} g_R^2 \right) \quad \text{and} \quad \phi_u = \frac{1}{\sqrt{2}} \log(U_1 + \bar{U}_1)$$

5. Conclusions

- In this talk I first review the minimal no-scale model based on

$$\mathcal{M}_n = SU(1, 1 + n)/U(1) \times SU(1 + n)$$

which is classically equivalent to the \mathcal{R}^2 coupled in a scale invariant matter.

- The stringy extension consists to include stringy moduli fields, namely, the dilaton and the complex structure moduli, S and U_I .

The scalar manifold is extended by the factor:

$$\mathcal{K}_n = \frac{SU(1, 1)_S}{U(1)} \times \frac{SU(1, 1)_{U_1}}{U(1)} \times \frac{SU(1, 1)_{U_2}}{U(1)} \times \frac{U(1, 1)_{U_3}}{U(1)}$$

- The presence of the additional moduli turns out to be crucial since both susy and R -symmetry can be spontaneously broken in the global Minkowski vacuum after the inflationary transition.

- The R -symmetry acts non trivially on the non perturbative superpotential which involves flux terms and the non-perturbative exponential factor: $\hat{w}(S, U_I) e^{-\beta S}$.
- The semi-classical R -symmetry becomes non-anomalous at the quantum level if the Peccei-Quinn axion shift symmetries associated to the T, S, U_I moduli-fields are gauged consistently.
- For large initial values of $T + \bar{T}$ and $U + \bar{U}$ the extended theory can describe successfully inflationary transition from de Sitter to the flat Minkowski space.
- The susy is broken in both phases:
 - In the de Sitter by a Fayet-Iliopoulos D -term
 - In the flat global vacuum by the non-perturbative susy breaking with $w \neq 0$ which breaks spontaneously both susy and R -symmetry

- The effective low energy theory (after fixing S, U_I and $|\Phi^i|^2$) is identical to M_n no scale model with naturally small gravitino mass,

$$m_{3/2}^2 = \frac{|\Lambda|^6}{(T' + \bar{T}')^3}, \quad 2T' = 2T - \tilde{\xi}$$

T' and $m_{3/2}^2$ are undetermined at the (semi-)classical level.

Thank you for your attention

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